# Stat 411/511

### ASSUMPTIONS, OUTLIERS & LOG Oct 21 2015

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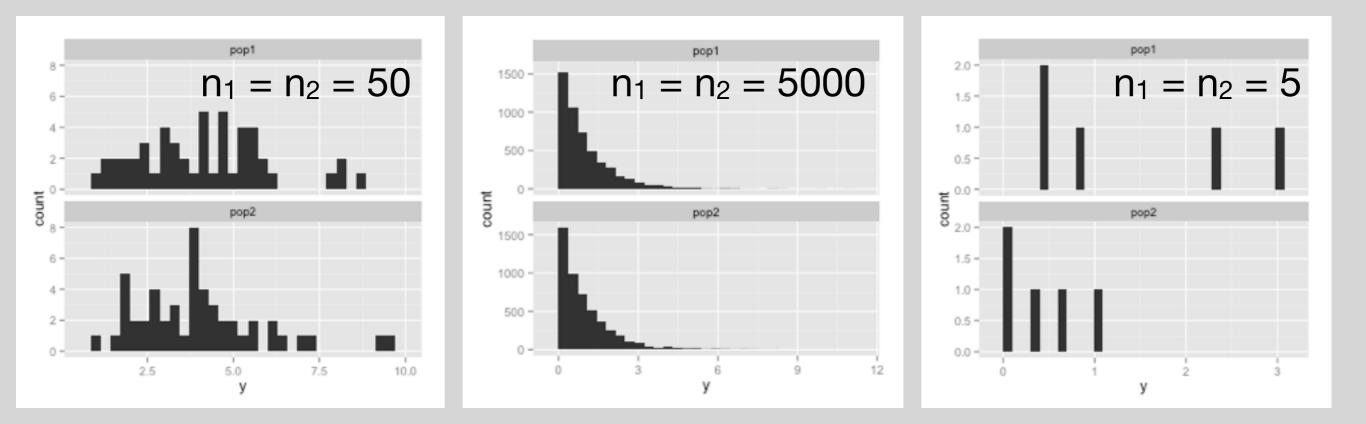
### Your turn

We are going to do a two sample t-test.

Put these datasets in order from:

"I would be very worried about the Normality assumption" to

"I would not be worried about the Normality assumption at all"



Today

The two other assumptions Outliers & Resistance The log transform

**Quiz:** you will need to calculate a pooled standard deviation, you will need a calculator/R.

# Equal standard deviations

# Equal population standard deviations

We assumed that  $\sigma_1 = \sigma_2$  and estimated the value with the pooled standard deviation.

If your **sample sizes** are roughly **equal**, the *t*-test will be fairly robust to **unequal population standard deviations**.

If your sample sizes are not equal, the *t*-test will not be valid with unequal population standard deviations.

Paired t-test: taking differences is probably not appropriate if the two groups have different spreads.

### Equal population SDs

**Check:** by looking at histograms of samples.

### Remedy:

use a transformation or or always use a Welch *t*-test

# Independence

### Independence

Observations must be independent of one another for *t*-tools to be valid.

If knowledge about one observation allows us to make a better guess about another observation, there is a lack of independence.

If there is dependence, t-tools give misleading results.

### Two common types of dependence

#### **Cluster effects**

There is some kind of subgroup within groups, and subjects in the same subgroup are more similar.

#### **Serial effects**

Measurements are made in time (or space) and observations made close in time (or space) are more similar.

### Independence

**Check**: read study design carefully, and look for sources of dependence.

### Remedy:

use more complicated methods (ST512)

The one solution we already know about is the paired t-test

Assumptions for using the randomization test

You have a randomized experiment (i.e. you have assigned subjects to treatment groups completely at random)

# Assumptions for using the two sample t-**test** instead of the randomization **test**

i.e. you want a p-value using the null hypothesis: there is no difference between the treatments

#### You have a randomized experiment

(i.e. you have assigned subjects to treatment groups completely at random) and

#### the samples aren't too non-Normal

(same deal as two sample t, you can get away with more non-Normality when you have more data)

Assumptions for using the two sample **CI** for difference in means instead of the randomization **CI** for an additive treatment effect

or you want a p-value using the null hypothesis: the additive treatment effect is zero.

#### You have a randomized experiment

(i.e. subjects were assigned to treatment groups completely at random) **and** 

#### the samples aren't too non-Normal

(same deal as two sample t, you can get away with more non-Normality when you have more data)

#### you assume the additive treatment model

(implies equal standard deviations of treatment outcomes)

# In practice, you look at all the same diagnostic plots as the two sample t-test

# Your turn

ANI MILI

Consider the numbers:

1, 2, 3, 5, 9, 10 What is their average? What is their median?

Imagine there was a mistake in recording the numbers and you were actually given:

1, 2, 3, 5, 9, 100

What is their average?

What is their median?

### Resistance

A procedure is **resistant** if it doesn't change much when a few subjects change.

- The average is not resistant.
- The median is resistant.
- The t-statistic is not resistant.

It can be sensitive to a few outlying observations

Outliers should not be deleted unless you know they are mistakes

If there are outliers retry the analysis without them.

If the conclusions don't change, leave them in and say so.

If the conclusions do change, investigate further, report both analyses.

#### OR

Use a **resistant** method (Chap 4)

## Log transform

Sometimes assumptions can be met by transforming the data.

A particularly useful transformation is the **logarithmic** transformation.

Useful, when variation increases with mean, or right skewed data.

Values must be positive to take logarithm.

Always use the same transformation on both groups.

### Cloud seeding

#### **Display 3.1**

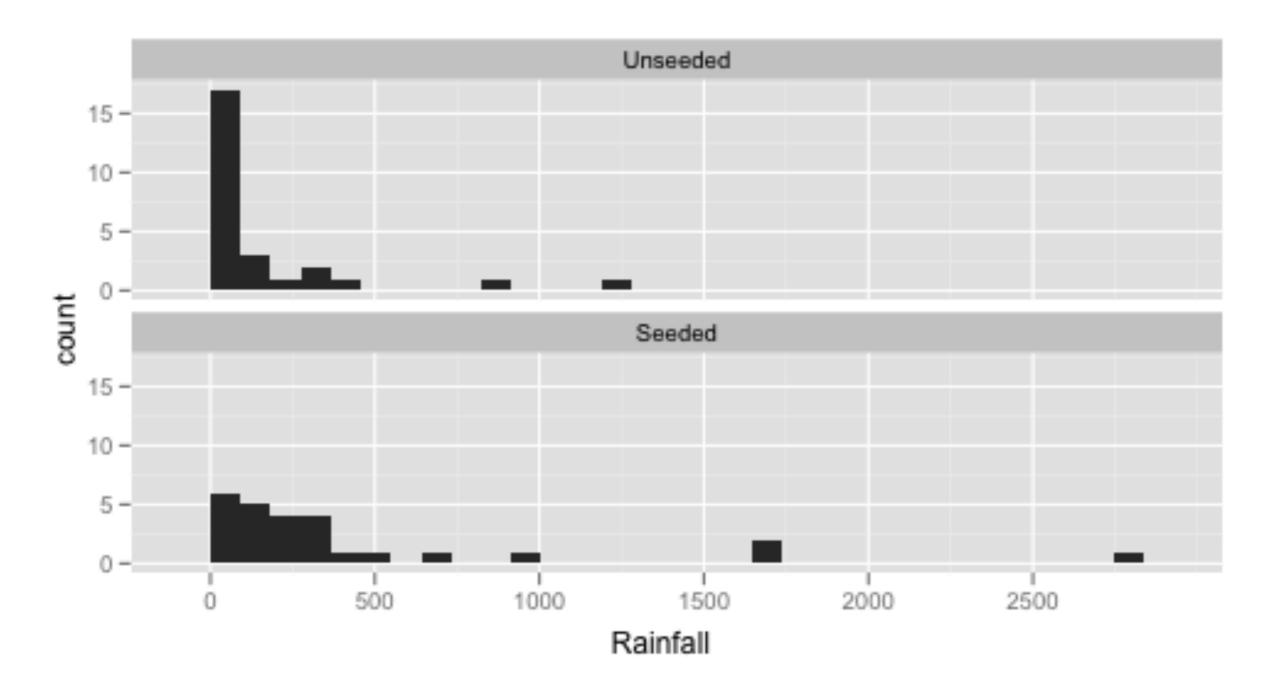
**p.** 57

#### **Rainfall** (acre-feet) for days with and without cloud seeding

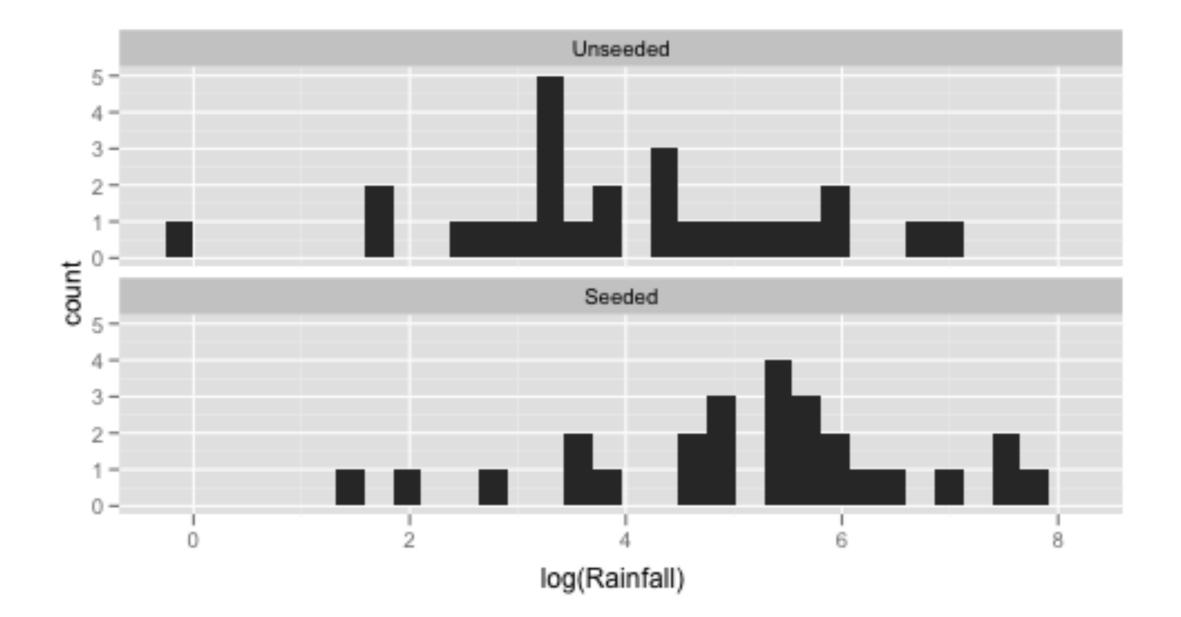
<u>Rainfall from unseeded days (<math>n = 26</math>)</u>									
1202.6 87.0 26.1	830.1 81.2 24.4	372.4 68.5 21.7	345.5 47.3 17.3	321.2 41.1 11.5	244.3 36.6 4.9	163.0 29.0 4.9	147.8 28.6 1.0	95.0 26.3	
<u>Rainfall from seeded days (<math>n = 26</math>)</u>									
2745.6 274.7 115.3	1697.8 274.7 92.4	1656.0 255.0 40.6	978.0 242.5 32.7	703.4 200.7 31.4	489.1 198.6 17.5	430.0 129.6 7.7	334.1 119.0 4.1	302.8 118.3	

#### Randomized experiment

qplot(Rainfall, data = case0301) +
facet\_wrap(~ Treatment, ncol = 1)



qplot(log(Rainfall), data = case0301)
+ facet\_wrap(~ Treatment, ncol = 1)



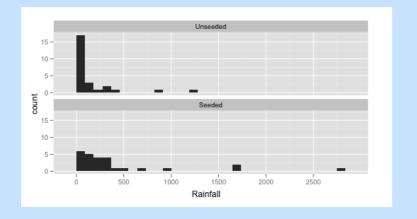
#### details on Mon

# Using the log transform

log transform

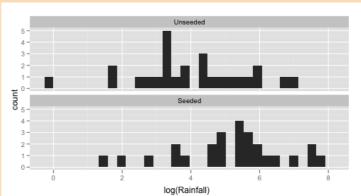
data

original scale acre feet of rainfall



back transform estimates and confidence intervals but **not** p-values

#### log scale log(acre feet of rainfall)



#### Recheck assumptions if things aren't improved, don't proceed

# Conduct analysis (t-tests etc.)

Two Sample t-test

t-tests over here tell us about **differences in means** of the populations of **log response** 

#### Make interpretations

With 95% confidence seeding clouds increases rainfall between 1.27 and 7.74 times that of unseeded clouds.

once back transformed those t-tests tell us about **ratios of medians** of the populations of **response**